

Test Suite for the Maxima Plugin

[Maxima](#)

$t_0 := \text{time}(0)$

All formatted labels on the right margin should be green (pass).

MaximaControl("restart")="Restart complete."

[-] Test functions

Maxima version

| | |
|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------|
| $T := \text{Test} \left(\text{M} (" \$args(\text{build_info}()) \$"); \left\{ \begin{array}{l} "5.34.1" \\ "2014-11-11 09:57:09" \\ "i686-pc-mingw32" \\ "GNU Common Lisp (GCL)" \\ "GCL 2.6.11" \end{array} \right. \right)$ | <div style="border: 1px solid black; background-color: green; color: white; padding: 2px; display: inline-block;">pass</div> T |
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Alternatives for internal functions

Maxima provides alternatives to the functions `int()`, `diff()`, `lim()`, `det()` and `sum()`

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| $T := \text{Test} (\text{Diff} (\text{sech} (x)); -\text{sech} (x) \cdot \tanh (x))$ | <div style="border: 1px solid black; background-color: green; color: white; padding: 2px; display: inline-block;">pass</div> T |
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| | |
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| $T := \text{Test} (\text{Diff} (\text{sech} (x); x); -\text{sech} (x) \cdot \tanh (x))$ | <div style="border: 1px solid black; background-color: green; color: white; padding: 2px; display: inline-block;">pass</div> T |
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| | |
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| $T := \text{Test} (\text{Diff} (\text{sech} (x); x; 2); (\tanh (x) - \text{sech} (x)) \cdot (\tanh (x) + \text{sech} (x)) \cdot \text{sech} (x))$ | <div style="border: 1px solid black; background-color: green; color: white; padding: 2px; display: inline-block;">pass</div> T |
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| | |
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| $T := \text{Test} (\text{Int} (\sin (x); x); -\cos (x))$ | <div style="border: 1px solid black; background-color: green; color: white; padding: 2px; display: inline-block;">pass</div> T |
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| | |
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| $T := \text{Test} \left(\text{Int} \left(10 \frac{N}{m}; x; 0; 2 m \right); 20 N \right)$ | <div style="border: 1px solid black; background-color: green; color: white; padding: 2px; display: inline-block;">pass</div> T |
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| $T := \text{STest} \left(\text{Lim} \left(\frac{x^2}{x}; x; \infty \right); "\infty" \right)$ | <div style="border: 1px solid black; background-color: green; color: white; padding: 2px; display: inline-block;">pass</div> T |
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| $T := \text{Test} \left(\text{Det} \left(a \cdot \begin{bmatrix} 1 & 2 \\ b & 3 \end{bmatrix} \right); a^2 \cdot (3 - 2 \cdot b) \right)$ | <div style="border: 1px solid black; background-color: green; color: white; padding: 2px; display: inline-block;">pass</div> T |
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| | |
|--------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------|
| $T := \text{Test} \left(\text{Sum} (j; j; 1; n); \frac{n \cdot (1 + n)}{2} \right)$ | <div style="border: 1px solid black; background-color: green; color: white; padding: 2px; display: inline-block;">pass</div> T |
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Wrapping of the internal functions (in order to use their operator representation)

| | | |
|------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------|--------|
| $\text{M} (\text{sech} (x))' = -\text{sech} (x) \cdot \tanh (x)$ | <p>"Request: diff(sech(x), x, 1); Answer: (%47) -sech(x)*tanh(x) (%i48) Received bytes: 32 SMATH get: "</p> | Maxima |
|------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------|--------|

| | | |
|-------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------|-------|
| $\text{M} \left(\frac{d}{dx} \text{sech} (x) \right) = -\text{sech} (x) \cdot \tanh (x)$ | <p>"Request: -sech(x)*tanh(x); Answer: (%49) -sech(x)*tanh(x) (%i50) Received bytes: 32 SMATH get: "</p> | SMATH |
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| | | |
|--------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------|--------|
| $\text{M} \left(\int \sin (x) dx \right) = -\cos (x)$ | <p>"Request: integrate(sin(x), x); Answer: (%51) -cos(x) (%i52) Received bytes: 23 SMATH get: "</p> | Maxima |
|--------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------|--------|

$\int_0^{2m} 10 \frac{N}{m} dx = \frac{20 kg}{s^2}$ MaximaLog(■) = "Request: 20*%unitkg/(%units^2); SMath, wrong Answer: (%o53) 20*%unitkg/%units^2 (%i54) Received bytes: 35 SMath get: "

$\int_0^b q dx = b \cdot q$ MaximaLog(■) = "Request: integrate(q,x,0,b); Maxima Answer: (%o57) b*q (%i58) Received bytes: 19 SMath get: "

$\lim_{x \rightarrow \infty} \frac{x^2}{x} = \infty$ MaximaLog(■) = "Request: limit((x^2)/x,x,inf); Maxima Answer: (%o59) inf (%i60) Received bytes: 19 SMath get: "

$\left| \begin{vmatrix} 1 & 2 \\ b & 3 \end{vmatrix} \right| = a^2 \cdot (3 - 2 \cdot b)$ MaximaLog(■) = "Request: determinant(a*matrix([1,2],[b,3])); Maxima Answer: (%o61) 3*a^2-2*a^2*b (%i62) Received bytes: 29 SMath get: "

$\sum_{j=1}^n j = \blacksquare$ MaximaLog(■) = "Request: determinant(a*matrix([1,2],[b,3])); Maxima Answer: (%o61) 3*a^2-2*a^2*b (%i62) Received bytes: 29 SMath get: "

Maxima is not called at all
 lastError = "n - not defined."

Unit handling

T := Test $\left(\int_0^{2m} 10 \frac{N}{m} dx ; 20 N \right)$ Fail due to wrong evaluation by SMath fail
 T

T := Test $(2m + 3 km ; 3002 m)$ pass
 T

T := Test (Solve(a + 3 m = 500 cm ; a) ; (a = 2 m)) pass
 T

$x_0 := 10 mm \quad y_0 := 50 mm \quad \varepsilon_0 := 0,05$
 $\varepsilon(x) := \varepsilon_0 \cdot \left(\frac{x}{x_0}\right) \quad y(x) := y_0 \cdot \left(\frac{x}{x_0}\right)^2$

T := Test $\left(\int_0^{x_0} \varepsilon(x) \cdot \sqrt{1 + \left(\frac{d}{dx} y(x)\right)^2} dx ; \frac{m \cdot \left(-1 + 101 \frac{3}{2}\right)}{600000} \right)$ pass
 T

Translation tests

T := Test $(\text{ΑΓΔΘΛΞ}_{\text{ΠΣΦΨΩ}} ; \text{ΑΓΔΘΛΞ}_{\text{ΠΣΦΨΩ}})$ pass
 T

T := Test $(\alpha\beta\gamma\delta\varepsilon\zeta\eta\theta\iota\kappa_{\lambda\mu\nu\xi\omicron\rho\sigma\tau\upsilon\phi\chi\psi\omega} ; \alpha\beta\gamma\delta\varepsilon\zeta\eta\theta\iota\kappa_{\lambda\mu\nu\xi\omicron\rho\sigma\tau\upsilon\phi\chi\psi\omega})$ pass
 T

T := Test $\left(\left\{ \begin{matrix} "a b \\ abc \end{matrix} \right\} ; \left\{ \begin{matrix} "a b \\ abc \end{matrix} \right\} \right)$ pass
 T

T := Test $(\text{"äöüß"} ; \text{"äöüß"})$ pass
 T

T := Test $(\text{"a+b"} ; \text{"a+b"})$ pass
 T

T := Test $(\text{strrep("a\b" ; "\ " ; "/")} ; \text{"a/b"})$ pass

T:= Test (\mathcal{M} ("a\\b") ; "a\\b")

T
pass

T:= Test (\mathcal{M} ("\$a\\b\$") ; "a\\b")

T
pass

T:= Test (\mathcal{M} (a + "\$b_c\$" + d) ; d + b_c + a)

T
pass

T:= Test (\mathcal{M} ("\$[x,y]\$") ; $\begin{cases} x \\ y \end{cases}$)

T
pass

T:= Test (\mathcal{M} ("\$[[x=1,y=2],[x=2,y=3]]\$") ; $\begin{cases} x=1 \\ y=2 \\ x=2 \\ y=3 \end{cases}$)

T
pass

T:= Test (\mathcal{M} ("\$2.1e100\$") ; $2,1 \cdot 10^{+100}$)

pass
T

T:= Test (\mathcal{M} ("\$2.1b100\$") ; $2,1 \cdot 10^{100}$)

pass
T

T:= Test (\mathcal{M} ($2 \cdot \pi$) ; $2 \cdot \pi$)

pass
T

T:= Test (\mathcal{M} ($\sin(i)$) ; $i \cdot \sinh(1)$)

pass
T

T:= Test (\mathcal{M} ($e^i \cdot e^i$) ; $e^i \cdot e^i$)

pass
T

T:= Test (\mathcal{M} ($2,3 \cdot \pi$) ; $2,3 \cdot \pi$)

pass
T

T:= Test (\mathcal{M} (dummy (a ; b)) ; dummy (a ; b))

pass
T

T:= Test (\mathcal{M} ($\begin{bmatrix} 1 & 2 \\ x & y & a \end{bmatrix}$) ; $\begin{bmatrix} 1 & 2 \\ x & y & a \end{bmatrix}$)

pass
T

T:= Test (\mathcal{M} ($\begin{bmatrix} "1" & 2 \\ x & y & a \end{bmatrix}$) ; $\begin{bmatrix} "1" & 2 \\ x & y & a \end{bmatrix}$)

pass
T

T:= Test (\mathcal{M} (v_k) ; v_k) Vector indices

pass
T

T:= Test (\mathcal{M} ($M_{j k}$) ; $M_{j k}$) Matrix indices

pass
T

T:= Test (\mathcal{M} ($a \leq b$) ; $a \leq b$) Boolean and relational operators

pass
T

T:= Test (\mathcal{M} ($a \geq b$) ; $a \geq b$)

pass
T

T:= Test (\mathcal{M} ($(a \neq b)$) ; $(a \neq b)$)

pass
T

T:= Test (\mathcal{M} ($a \wedge b$) ; $a \wedge b$)

pass
T

T:= Test (\mathcal{M} ($a \vee b$) ; $a \vee b$)

pass
T

T:= Test (\mathcal{M} ($\left[\left[\begin{cases} x=1 \\ y=2 \end{cases} \begin{cases} x=2 \\ y=3 \end{cases} \right] ; \left[\begin{cases} x=1 \\ y=2 \end{cases} \begin{cases} x=2 \\ y=3 \end{cases} \right] \right)$) matrices of lists

pass
T

T:= Test (\mathcal{M} ($\left\{ f \left(\begin{cases} a \\ b \end{cases} ; \begin{cases} c \\ d \end{cases} \right) ; \left\{ f \left(\begin{cases} a \\ b \end{cases} ; \begin{cases} c \\ d \end{cases} \right) \right\}$) Lists and functions with multiple arguments

pass
T

T:=Test (M ((({ f(x ; y) 2 } , { f(x ; y) 2 }) ; "a" x_y a) ; "a" x_y a) Matrices, lists and functions with multiple arguments pass
T

c:=a*b T:=STest (M (c^2) ; "a^2*b^2") pass
T

T:=Test (M (string(log_y(x))) ; "log(x)/log(y)") pass
T

T:=Test (M (string({ a }) ; "[a,b]") pass
T

Function ODE.2 and handling of Maxima asking questions about signs

T:=Test (ODE_2 (((d^2 w(t)+omega^2*w(t)=0) ; w(t) ; t) ; { "omega is assumed to be positive." w(t)=k1*e^(i*omega*t)+k2*e^(-i*omega*t) }) pass
T

T:=Test (M (assume(omega>0)) ; { (omega>0) }) pass
T

T:=Test (Assign (ODE_2 (((d^2 w(t)+omega^2*w(t)=0) ; w(t) ; t) ; k1*sin(omega*t)+k2*cos(omega*t)) pass
T

Functions Solve(), Algsys(), LinSolve() and Assign()

T:=Test (Assign (Solve (((x^2+(3*x)*y+y^2=0) ; [x])) ; { -3+sqrt(5)/2 -7+3*sqrt(5)/2 }) Clear(x ; y)=1 pass
T

eq_1:=(x^2+(3*x)*y+y^2=0) eq_2:=(3*x+y=1)

T:=Test (Algsys ((eq_1) ; [x]) ; { (x = (-3+sqrt(5))/2) (x = (3+sqrt(5))/2) (y = (-7+3*sqrt(5))/2) (y = (-7+3*sqrt(5))/2) }) pass
T

eq_1:=(x+z=y) eq_2:=(2*a)*x-y=2*a^2 eq_3:=(y-(2*z)=2)

T:=Test (Unknowns (eq) ; [a]) pass
T

T:=Test (LinSolve (eq ; [x] ; { (x=(1+a)) (y=2*a) (z=(-1+a)) }) pass
T

Cross product with scaled vectors

a:= [a_1] b:= [b_1] c:= [c_1] (lambda*a)*b = ■ T:=Test (M ((lambda*a)*b) ; { lambda*(a_2*b_3-a_3*b_2) lambda*(a_3*b_1-a_1*b_3) lambda*(a_1*b_2-a_2*b_1) }) pass
T

T:=Test (a*(b*c) ; a_1*(b_2*c_3-b_3*c_2)+a_2*(b_3*c_1-b_1*c_3)+a_3*(b_1*c_2-b_2*c_1)) pass
T

a*((lambda*b)*c) = ■ T:=Test (M (a*((lambda*b)*c)) ; lambda*((b_2*c_3-b_3*c_2)*a_1+(b_3*c_1-b_1*c_3)*a_2+(b_1*c_2-b_2*c_1)*a_3)) pass
T

Clear(a ; b ; c)=1

Handling of warnings and messages

```
T:=Test (Solve (cos (x)=1/sqrt(2); x) 2; (x=pi/4))
T:=Test (Axiom (integrate (|x-1|/x dx) -1 1); {"Principal Value"} -2)
T:=Test (Axiom (ilt ((2*(s-a)*(s+a))/(s^3*(b*s^2+a*(1-(a*b))))); s; t); {"a*b*(a*b-1) is assumed to be positive."} -2*(cosh(sqrt(a*b*(a*b-1))*t/b)/(a^3*b^2-2*a^2*b+a) + a*t^2/(a*b-1) + (a^3*b^2-
```

pass
T
pass
T

Back-translation of at()

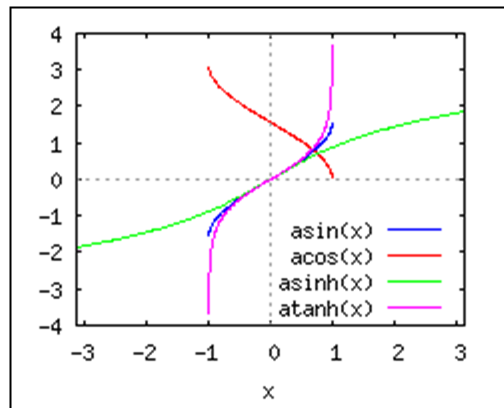
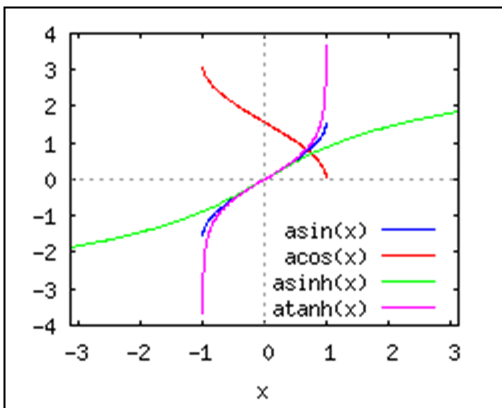
```
T:=Test (Axiom (laplace (d/dt delta(t); t; s); -d/dt delta(t)|t=0 + s^2 - delta(0)*s)
```

pass
T
pass
T

Plotting with plot2d

```
p:= (Axiom (set_plot_option (gnuplot_preamble "set key bottom right; set grid"))
(Axiom (set_plot_option (gnuplot_term "png small size 250, 200"))
(Axiom (plot2d (asin(x) acos(x) asinh(x) atanh(x)); (x (-pi pi)))
concat (Axiom (maxima_tempdir); "/" ; "maxplot.png")
```

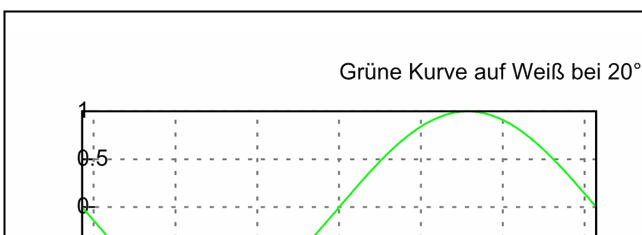
CurrentDirectory(DocumentDirectory(■))="C:\FHB\Software\SMath\Activebook\activebook\"

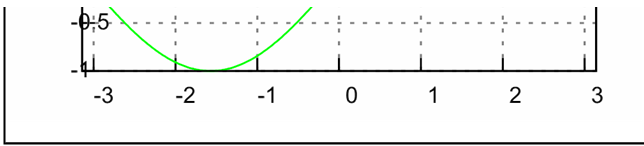


p "maxplotref.png"

Draw2D() with special characters and automatic temporary filename

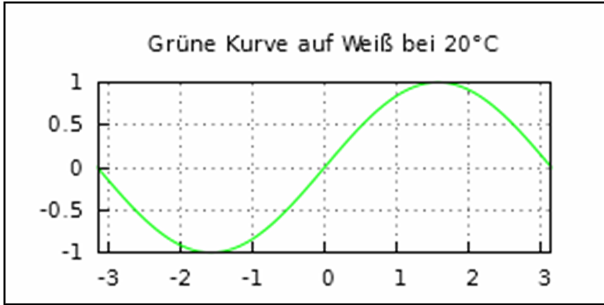
```
p:=Draw2D (title="Grüne Kurve auf Weiß bei 20°C" color=green explicit(sin(x); x; -pi; pi) grid=true; {300 150})
```





p

```
p:=Draw2D { title="Grüne Kurve auf Weiß bei 20°C",
  color=green,
  explicit(sin(x); x; -pi; pi),
  grid=true } ; "grün.png" ; { 300, 150 }
```



p

Result format of Eigenvalues and -vectors

```
T:=Test (ME eigenvalues ( [[ 100 50 ], [ 50 0 ] ] ); [ [ 50 - 25*2 (3/2), 25*2 (3/2) + 50 ], [ [ 1 -sqrt(2) - 1 ], [ 1 sqrt(2) - 1 ] ] ] )
```

pass
T

```
T:=Test (ME eigenvectors ( [[ 1 m 0 0 ], [ 0 3 0 ], [ 0 0 1 m ] ] ); [ [ 1 m 3 ], [ [ 1 0 0 ], [ 0 0 1 ], [ 0 1 0 ] ] ] )
```

pass
T

Translation of derivatives improved

diff(3) is used only if exponent is greater than 1

```
T:=STest (ME ( d/dx d/dy f(x; y) ); "diff(diff(f(x,y), y), x) ")
```

pass
T

```
T:=STest (ME ( d^2/dx^2 f(x; y) ); "diff(f(x,y), x, 2) ")
```

fail
T

```
T:=STest (Diff(f(x); x; 2); "diff(f(x,y), x, 2) ")
```

fail
T

```
T:=STest ( d/dx d/dy d/dz f(x; y; z); "diff(diff(diff(f(x,y,z), z), y), x) ")
```

pass
T

```
T:=Test (ME jacobian ( [ f(r; phi), g(r; phi) ]; [ r ], [ phi ] ); [ [ d/dr f(r; phi), d/dphi f(r; phi) ], [ d/dr g(r; phi), d/dphi g(r; phi) ] ] )
```

pass
T

Test of diff(1)

```
T:=Test (ME ((f(x)·g(x))'); f(x)·d/dx g(x) + g(x)·d/dx f(x)
```

pass
T

```
T:=Test (ME ((sin(x)·ln(x))'); sin(x)/x + cos(x)·ln(x)
```

pass
T

```
T:=Test (ME ((f(g(x)))'); d/dx f(g(x))
```

pass
T

```
T:=Test (ME ((sin(x^2))'); 2·x·cos(x^2)
```

pass

Function calls

f(a):= a²



T:= Test ( (f (b mm)) ; m² · $\frac{b^2}{1000000}$)  T

T:= Test ( (f ((b mm))) ; m² · $\frac{b^2}{1000000}$)  T


T:= Test ( (a_b_c_d) ; a_b_c_d)  T

T:= Test ( (string(a_b_c_d)) ; "a_b_c_d")  T

T:= Test ( (a_b,c,d) ; a_b,c,d)  T

T:= Test ( (string(a_b,c,d)) ; "a_%_b_%_c_%_d")  T



T:= Test ( (a_b,c) ; a_b,c)  T

T:= Test ( (string(a_b,c)) ; "a_%_b_%_c")  T

T:= Test ( ($\begin{Bmatrix} 1,2 \\ 2,3 \end{Bmatrix}$) ; $\begin{Bmatrix} 1,2 \\ 2,3 \end{Bmatrix}$)  T

Loading of abs_integrate


f(x):= x³ - (6 · x²) + 8 · x

T:= Test ( ($\int_0^3 |f(x)| dx$) ; $\frac{23}{4}$) This is numerically integrated by SMath before Maxima can have it.  T

T:= Test (Int (|f(x)| ; x ; 0 ; 3) ; $\frac{23}{4}$)  T

Definition in SMath and Maxima


T:= Test (MaximaDefine (A ; 3) ; 3)  T

T:= Test (A ; A) Variable A wird in SMath nicht definiert.  T

T:= Test ( ("\$A\$") ; 3)  T


Transfer of an existing SMath-Definition to Maxima

C:= $\begin{Bmatrix} 2 \\ 3 \end{Bmatrix}$ D:= 4 E:= 12 Definition in SMath

T:= Test (MaximaDefine (C ; D) ; $\begin{Bmatrix} 2 \\ 3 \\ 4 \end{Bmatrix}$)  T

T:= Test (MaximaDefine (E) ; 12)  T

T:= Test (E ; 12)  T

Clear (D ; C) = 1 Clear the definition in SMath  T

T:= STest (D · C ; "D*C")  T

T
 $T := \text{Test} \left(\text{\%M}(D \cdot C) ; \left\{ \begin{matrix} 8 \\ 12 \end{matrix} \right\} \right)$ Still available in Maxima pass

T
 $T := \text{Test} \left(\text{\%M}(\text{kill}(D ; C)) ; \text{done} \right)$ Clear the definitions in Maxima pass

T
 $T := \text{Test} \left(\text{\%M}(D \cdot C) ; C \cdot D \right)$ pass

T
 $T := \text{Test}(\text{MaximaDefine}(\text{fpprec} ; 40) ; 40)$ pass

T
 $T := \text{Test} \left(\text{\%M}(\text{bfloat}(\pi)) ; 3,141592653589793238462643383279502884197 \cdot 10^0 \right)$ pass

T
 $T := \text{Test}(\text{MaximaDefine}(\text{fpprec} ; 16) ; 16)$ pass

T
 $T := \text{Test} \left(\text{\%M}(\text{bfloat}(\pi)) ; 3,141592653589793 \cdot 10^0 \right)$ pass

T
 $T := \text{Test} \left(\text{\%M}(\text{split}("a,b" ; ", ")) ; \left\{ \begin{matrix} "a" \\ "b" \end{matrix} \right\} \right)$ pass

T
 $T := \text{Test} \left(\text{\%M} \left("\$at(\text{diff}(\text{delta}(y), y), y=0)\$" \right) ; \left. \frac{d}{d y} \text{delta}(y) \right|_{y=0} \right)$ pass

T
 $T := \text{Test} \left(\text{\%M} \left(\left. \frac{d}{d y} \text{delta}(y) \right|_{y=0} \right) ; \left. \frac{d}{d y} \text{delta}(y) \right|_{y=0} \right)$ pass

T
 $T := \text{Test} \left(\text{\%M}(x^{0,5}) ; x^{0,5} \right)$ pass

T
 $T := \text{Test} \left(\text{\%M}("\$%\$") ; x^{0,5} \right)$ fail

T

Access to Lapack functions

msg := $\text{\%M}(\text{load}(\text{lapack}))$

$M := \begin{bmatrix} 1 & 2 & 3 \\ 3,5 & 0,5 & 8 \\ -1 & 2 & -3 \\ 4 & 9 & 7 \end{bmatrix}$ $T := \text{Test} \left(\text{\%M}(\text{dgesvd}(M ; \text{true} ; \text{true})) ; \begin{matrix} 1 \\ \left\{ \begin{matrix} 14,47444340493696 \\ 6,386367492469741 \\ 0,452546537278426 \end{matrix} \right\} \end{matrix} \right)$ pass

$\text{time}(0) - t_0 = 22,351 \text{ s}$